## CHAPTER 1 -Essentials of GEOMETRy

In this chapter we address three Big IDEAS:

1) Describing geometric figures
2) Measuring geometric figures
3) Understanding equality and congruence

| Section: | 1 - 1 Identify Points, Lines, and Planes |
| :--- | :--- |
| Essential <br> Question | How do you name geometric figures? |

Warm Up:
$\square$
Key Vocab:

| Undefined Terms |  |  |
| :---: | :---: | :---: |
| A basic figure that is not defined in terms of other figures. |  |  |
| Point | An undefined term in geometry <br> Has no dimension - no length, width, or height. <br> Designates a location | A "Point $A$ " |
| Line | An undefined term in geometry <br> Has one dimension - length <br> A straight path that has no thickness and extends forever |  |
| Plane | An undefined term in geometry <br> Has two dimensions - length and width <br> A flat surface that has no thickness and extends forever in two dimensions | Plane $E F G$ or Plane $R$ |

## Defined Terms

Terms that can be described using other figures such as point or line

| Collinear Points | Points that lie on the same line. |  |
| :---: | :---: | :---: |
| Coplanar Points | Points that lie in the same plane. |  |
| Line Segment | Part of a line that consists of two points, called endpoints, and all points on the line that are between the endpoints. | $\mathrm{C}_{\overline{B C}}^{\mathrm{B}}$ |
| Ray | Half of a line that consists of one point called an endpoint and all points on the line that extend in one direction. |  |
| Opposite Rays | Collinear rays, with a common endpoint, extending in opposite directions. | $\overrightarrow{S R}$ and $\overrightarrow{S T}$ are opposite rays <br> $S$ is the common endpoint. |
| Intersection | The set of all points two or more figures have in common. |  |

## Show:

Ex 1:
a. Give two other names for $\overleftrightarrow{B D}$.
$\overleftrightarrow{D B}$ and $m$
b. Give another name for plane $T$. plane $A B E$, plane $B E C$, plane $A E C$
c. Name three points that are collinear.
$A, B, C$
d. Name four points that are coplanar.

$A, B, C, E$

## Ex 2:

a. Give another name for $\overline{P R}$.
$\overline{R P}$
b. Name all rays with endpoint $Q$. Which of these rays opposite rays?
$\overrightarrow{Q P}, \overrightarrow{Q R}, \overrightarrow{Q T}, \overrightarrow{Q S}$;

are
$\overrightarrow{Q T}$ and $\overrightarrow{Q S}, \overrightarrow{Q P}$ and $\overrightarrow{Q R}$ are opposite rays.

| Section: | $\mathbf{1 - 2}$ Use Segments and Congruence |
| :--- | :--- |
| Essential <br> Question | What is the difference between congruence and equality? |

## Warm Up:

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Key Vocab:

| Postulate or Axiom | A rule that is accepted without proof |
| :---: | :---: |
| Theorem | A rule that can be proven |
| Between | When three points are collinear, you can say one point is between the other two. |
| Congruent Segments | Line segments that have the same length. |
|  | Lengths are equal Segments are congruent <br> $A B=C D$ (is equal to) $\overline{A B} \cong \overline{C D}$ (is congruent to) <br> a number $=$ a number A segment $\cong$ a segment |

Postulates:

| Ruler Postulate |  |
| :---: | :---: |
| Allows for the creation of a measuring system. |  |
| The points on a line can be matched one to one with the real numbers. <br> The real number that corresponds to a point is the coordinate of the point. |  |
| The distance between points $A$ and $B$, written $A B$, is the absolute value of the difference of the coordinates of $A$ and $B$. |  |


| Segment Addition Postulate |  |  |
| :---: | :---: | :---: |
| The sum of the parts equals the whole |  |  |
| If <br> $B$ is between $A$ and $C$, | then $A B+B C=A C .$ |  |
| If $A B+B C=A C$ | then <br> $B$ is between $A$ and $C$. |  |

## Show:

Ex 1: The cities shown on the map lie approximately in a straight line. Use the given distances to find the distance from Bismarck to Fargo. 190 mi


Ex 2: Find CD. 42-17=25


Ex 3: Graph the points $X(-2,-5), Y(-2,3), W(-4,3)$, and $Z(4,3)$ in a coordinate plane. Are $\overline{X Y}$ and $\overline{W Z}$ congruent?


$$
\overline{X Y} \cong \overline{W Z}
$$

Ex 4: Find the value of $x$. Then find $M N$.


| Section: | $\mathbf{1 - 3}$ Use Midpoint and Distance Formulas |
| :--- | :--- |
| Essential <br> Question | How do you find the distance and the midpoint between two <br> points in the coordinate plane? |

Warm Up:
$\square$

Key Vocab:

| Midpoint | The point that divides the segment <br> into two congruent segments. | Mis the midpoint of $\overline{A B}$ |
| :--- | :--- | :--- |
| Segment <br> Bisector | A point, ray, line, line segment, or <br> plane that intersects the segment at <br> its midpoint. |  |

## Key Concepts:

| Midpoint Formula |  |
| :---: | :---: |
| If <br> $A\left(x_{1}, y_{1}\right)$ and $B\left(x_{2}, y_{2}\right)$ are points on coordinate plane, | then <br> the midpoint $M$ of $\overline{A B}$ has coordinates $\left(\frac{x_{1}+x_{2}}{2}, \frac{y_{1}+y_{2}}{2}\right)$ |
|  |  |


| Distance Formula |  |
| :---: | :---: |
| If $A\left(x_{1}, y_{1}\right)$ and $B\left(x_{2}, y_{2}\right)$ are points in coordinate plane, | then <br> the distance between $A$ and $B$ is $A B=\sqrt{\left(x_{2}-x_{1}\right)^{2}+\left(y_{2}-y_{1}\right)^{2}}$ |
|  |  |

## Show:

Ex 1: The figure shows a gate with diagonal braces. $\overline{M O}$ bisects $\overline{N P}$ at $Q$. If $\mathrm{PQ}=22.6$ in., find $P N$. By the definition of a segment bisector $P N=45.2$ in


Ex 2: Point $S$ is the midpoint of $\overline{R T}$. Find $S T$.


$$
\begin{aligned}
5 x-2 & =3 x+8 \\
2 x & =10 \\
x & =5
\end{aligned}
$$

$$
S T=3(5)+8=23
$$

Ex 3: Find $P Q$ given the coordinates for its endpoints are $P(2,5)$ and $Q(-4,8)$. Approximate answer rounded to the nearest hundredth.

$$
\begin{aligned}
P Q & =\sqrt{(-4-2)^{2}+(8-5)^{2}} \\
& =\sqrt{36+9} \\
& =\sqrt{45} \approx 6.71
\end{aligned}
$$

Ex 4: The endpoints of $\overline{G H}$ are $G(7,-2)$ and $H(-5,-6)$. Find the coordinates of the midpoint $P$.

$$
\left(\frac{7-5}{2}, \frac{-2--6}{2}\right)=(1,-4)
$$

| Section: | $\mathbf{1 - 4}$ Measure and Classify Angles |
| :--- | :--- |
| Essential <br> Question | How do you identify whether an angle is acute, right, obtuse, or <br> straight? |

Warm Up:
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Key Vocab:

| Angle | Two different rays with the same <br> endpoint <br> Notation: $\square B A C, \square C A B, \square A, \square 1$ <br> $\angle B A C, \angle C A B, \angle A, \angle 1$ |
| :--- | :--- | :--- |
| Sides | The rays are the sides of the angle <br> Notation: $\overrightarrow{A B}, \overrightarrow{A C}$ |
| Vertex | The common endpoint of the rays |


| Angle Bisector | A ray that divides an angle into two <br> congruent angles. |
| :--- | :--- | :--- | :--- |
|  | *segment bisector $\neq$ angle bisector* |$\underset{Y W}{ }$



Postulate:


## Show:

Ex 1: Name each angle that has N as a vertex. $\angle M N O, \angle O N P, \angle M N P$


Ex 2: Use the diagram to find the measure of each angle and classify the angle.

a. $\angle D E C \_90^{\circ}$ Right
b. $\angle D E A \_180^{\circ}$ Straight_
c. $\angle C E B \quad 20^{\circ}$ Acute $\qquad$
d. $\angle D E B$ $\qquad$ $110^{\circ}$ Obtuse

Ex 3: If $m \angle X Y Z=72^{\circ}$, find $m \angle X Y W$ and $m \angle Z Y W$.
By the Angle Addition Postulate:


$$
\begin{array}{r}
2 x-9+3 x+6=72 \\
5 x-3=72 \\
5 x=75 \\
x=15
\end{array}
$$

$$
\begin{aligned}
& m \angle X Y W=2(15)-9=21^{\circ} \\
& m \angle Z Y W=3(15)+6=51^{\circ}
\end{aligned}
$$

| Section: | $\mathbf{1 - 5}$ Describe Angle Pair Relationships |
| :--- | :--- |
| Essential <br> Question | How do you identify complementary and supplementary angles? |

Warm Up:
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## Key Vocab:

| Complementary Angles | Two angles whose sum is $90^{\circ}$ |  |
| :---: | :---: | :---: |
| Supplementary Angles | Two angles whose sum is $180^{\circ}$ | Adjacent <br> Non-adjacent |
| Adjacent Angles | Two angles that share a common vertex and side, but have no common interior points |  |
| Linear Pair | Two adjacent angles whose noncommon sides are opposite rays | $\stackrel{1}{\longleftrightarrow}$ |
| Vertical Angles | Two angles whose sides form two pairs of opposite rays <br> Examples: $\angle 1$ and $\angle 3$ $\angle 2$ and $\angle 4$ |  |

## Show:

Ex 1: In the figure, name a pair of complementary angles, a pair of supplementary angles, and a pair of adjacent angles. $\angle G H I, \angle J L K ; \angle G H I, \angle K L M ; \angle J L K, \angle K L M$


Ex 2: a. Given that $\angle 1$ is a complement of $\angle 2$ and $m \angle 1=17^{\circ}$, find $m \angle 2.73^{\circ}$
b. Given that $\angle 3$ is a supplement of $\angle 4$ and $m \angle 3=119^{\circ}$, find $m \angle 4.61^{\circ}$

Ex 3: Two roads intersect to form supplementary angles, $\angle X Y W$ and $\angle W Y Z$. Find $m \angle X Y W$ and $m \angle W Y Z .76^{\circ}, 104^{\circ}$


Ex 4: Identify all of the linear pairs and all of the vertical angles in the figure.


Linear pairs: $\angle 2$ and $\angle 3 ; \angle 1$ and $\angle 3$
Vertical angles: $\angle 1$ and $\angle 3$

Ex 5: Two angles form a linear pair. The measure of one angle is 3 times the measure of the other angle. Find the measure of each angle.

| $3 x+x$ | $=180$ |
| ---: | :--- |
| $4 x$ | $=180$ |
| $x$ | $=45^{\circ}$ |
| $3 x$ | $=135^{\circ}$ |

Ex 6: The measure of one angle is 7 times the measure of its complement. Find the measure of each angle.

$$
\begin{aligned}
7 x+x & =90 \\
8 x & =90 \\
x & =11.25^{\circ} \\
7 x & =78.75^{\circ}
\end{aligned}
$$

| Section: | $\mathbf{1 - 6} \quad$ Classify Polygons |
| :--- | :--- |
| Essential <br> Question | How do you classify polygons? |

## Warm Up:

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## Key Vocab:

| Polygon | A closed plane figure with three or <br> more sides <br> each side intersects exactly two <br> sides, one at each endpoint, so that <br> no two sides with a common <br> endpoint are collinear |  |
| :--- | :--- | :--- |
| Sides | Each line segment that forms a <br> polygon | Sides: $\overline{A B}, \overline{B C}, \overline{C D}, \overline{D E}$, and $\overline{A E}$ |
| Vertex | Each endpoint of a side of a polygon |  |
| Convex |  |  |


| Concave | A polygon with one or more interior <br> angles measuring greater than $180^{\circ}$ <br> Opposite of convex |  |
| :--- | :--- | :--- |
| n-gon | A polygon with $n$ sides | Example: A polygon with 14 sides <br> is a 14-gon |
| Equilateral | A polygon with all of its sides <br> congruent | A polygon with all of its interior <br> angles congruent |
| Equiangular |  |  |
| Regular | A convex polygon that has all sides <br> and all angles congruent |  |

## Show:

Ex 1: Tell whether each figure is a polygon. If it is, tell whether it is concave or convex.


Yes; Convex
b.


Yes; Concave

Ex 2: Classify the polygon by the number of sides. Tell whether the polygon is equilateral, equiangular, or regular. Explain your reasoning.
a.


Triangle; only 2 sides congruent, only 2 angles congruent, so not equilateral, not equiangular, not regular.


Hexagon; equilateral, equiangular, regular


Quadrilateral; equilateral, not equiangular, so not regular

Ex 3: A rack for billiard balls is shaped like an equilateral triangle. Find the length of a side.


$$
\begin{aligned}
6 x-4 & =4 x+2 \\
2 x & =6 \\
x & =3
\end{aligned}
$$

