

SHOW ALL WORK!

1. Which of the following are expressions?

A. $3x+2$

B. $\frac{2x^2-4}{10}$

C. $2x-7y=32$

Simplify AND give the restrictions.

2. $\frac{-3x^2+20x+7}{2x^2-11x-21}$

$$\frac{-(3x^2-20x-7)}{(2x+3)(x-7)}$$

$$\frac{-(3x+1)(x-7)}{(2x+3)(x-7)} = \frac{-(3x+1)}{2x+3}$$

Domain: All Real #'s except $x=7, -\frac{3}{2}$

3. $\frac{2x^2-5x-12}{2x^2+5x+3} \rightarrow \frac{(2x+3)(x-4)}{(2x+3)(x+1)}$

$$\frac{x-4}{x+1}$$

Domain: All Real #'s except $x=-1, -\frac{3}{2}$

Perform the indicated operation(s) and simplify completely.

4. $\frac{4-x^2}{x^2+2x-8} \cdot \frac{x^2-11x+28}{x^2-5x-14}$

$$\frac{-(x+2)(x-2)}{(x-2)(x+4)} \cdot \frac{(x-7)(x-4)}{(x-7)(x+2)}$$

$$\frac{-(x-4)}{x+4}$$

5. $\frac{z^2-81}{z^2-16} \div \frac{z^2-z-20}{z^2+5z-36}$

$$\frac{z^2-81}{z^2-16} \cdot \frac{z^2+5z-36}{z^2-z-20}$$

$$\frac{(z+9)(z-9)}{(z+4)(z-4)} \cdot \frac{(z+9)(z-4)}{(z-5)(z+4)}$$

$$\frac{(z+9)^2(z-9)}{(z+4)^2(z-5)}$$

Perform the indicated operation(s) and simplify completely.

$$6. \frac{2}{x-2} + \frac{x}{-x+2} \cdot \frac{-1}{-1}$$

$$\frac{2}{x-2} + \frac{-x}{x-2}$$

$$\frac{2-x}{x-2}$$

$$\frac{-(x-2)}{x-2}$$

$$\boxed{-1}$$

$$\frac{x+5}{x+5} \cdot \frac{2x+1}{x-3} + \frac{x+2}{x+5} \cdot \frac{x-3}{x-3}$$

$$\frac{2x^2+x+10x+5}{(x+5)(x-3)} + \frac{x^2+2x-3x-6}{(x+5)(x-3)}$$

$$\boxed{\frac{3x^2+10x-1}{(x+5)(x-3)}}$$

$$8. \frac{2+\frac{1}{x}}{4x-\frac{1}{x}}$$

$$9. \frac{c^{-1}}{a^{-1}+b^{-1}} = \frac{\frac{1}{c}}{\frac{1}{a}+\frac{1}{b}}$$

Method 1: $\frac{x}{x} \cdot \frac{2+\frac{1}{x}}{1} \div \frac{x}{x} \cdot \frac{4x-\frac{1}{x}}{1} \cdot \frac{1}{x}$

$$\frac{2x+1}{x} \div \frac{4x^2-1}{x}$$

$$\frac{2x+1}{x} \cdot \frac{x}{4x^2-1}$$

$$\frac{2x+1}{x} \cdot \frac{x}{(2x+1)(2x-1)}$$

$$\boxed{\frac{1}{2x-1}}$$

Method 1:

$$\frac{1}{c} \div \frac{b}{b} \frac{1}{a} + \frac{1}{b} \cdot \frac{a}{a}$$

$$\frac{1}{c} \div \frac{b+a}{ab}$$

$$\frac{1}{c} \cdot \frac{ab}{b+a}$$

$$\boxed{\frac{ab}{c(b+a)}}$$

Method 2:

$$\frac{2+\frac{1}{x}}{4x-\frac{1}{x}} \cdot \frac{x}{x}$$

$$\frac{2x+1}{4x^2-1}$$

$$\frac{2x+1}{(2x+1)(2x-1)}$$

$$\boxed{\frac{1}{2x-1}}$$

Method 2:

$$\frac{\frac{1}{c}}{\frac{1}{a}+\frac{1}{b}} \cdot \frac{abc}{abc}$$

$$\frac{ab}{bc+ac}$$

$$\boxed{\frac{ab}{c(b+a)}}$$